

Newchurch Community Primary School

Mathematics Policy and Building to written methods













Linked Policy Documents:

- Visual Calculation Policy
- Visual Fractions Policy
- Marking and Feedback Policy

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Introduction

The Mathematics framework provides a structured and systematic approach to teaching number. There is a considerable emphasis on teaching mental calculation strategies and speaking and listening activities. Up to the age of 9 (Year 4) informal written recording should take place regularly and is an important part of learning and understanding. More formal written methods should follow only when the child is able to use a wide range of mental calculation strategies. This will help communicate methods and solutions.

Why do we need this policy?

- Consistency in methods taught throughout the school.
- Progression from informal / practical methods of recording to written methods for each of the four operations.
- An aid to parent's understanding in their child's stages of learning.

Reasons for using written methods

- To aid mental calculation by writing down some of the numbers and answers involved
- To make clear a mental procedure for the pupil
- To help communicate methods and solutions
- To provide a record of work to be done
- To aid calculation when the problem is too difficult to be done mentally
- To develop and refine a set of rules for calculation

How mathematics is taught at Newchurch:

The aim of the mathematics approach is to develop the children's mental calculation confidence before moving onto the written methods of formal mathematics. The lessons will be differentiated to meet the needs of the children, however they will work within the expectations of the National Curriculum.

The children will meet mathematics in three main formats:

1. Fluency – This is be the children's ability to perform the

base standard of the target e.g. perform a written

calculation method.

2. Reasoning - The children will apply their knowledge of number

and methods to more contextual problems including

word problems.

3. Problem solving - The children will investigate more expansive

challenges which employ their mathematics

knowledge. This can include open-ended tasks and those linked to other areas of the curriculum e.g.

mathematics within science.

Marking and Feedback will support the children in progressing between these three stages. They will be supported in their learning through the use of concrete manipulatives (objects), visual support (images) and finally abstract methodology.

Whole school approach

We have developed a consistent approach to the teaching of written calculation methods. This will establish continuity and progression throughout the school.

Different mental methods will be established in Key Stage 1 and built on as the children progress into Key Stage 2. These are shown below and will be based on a solid understanding of place value in number.

Things to remember for Key Stage One

- i. Remembering number facts and recalling them without hesitation e.g. pairs of numbers that make 10
- ii. Doubles and halves to 20
- iii. Using known facts to calculate unknown facts

e.g. 6 + 6 = 12 therefore 6 + 7 = 1324 + 10 = 34 therefore 24 + 9 = 33

iv. Understanding and using relationships between addition and subtraction to find answers and check results

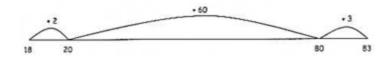
e.g. 14 + 6 = 20 therefore 20 - 6 = 14

v. Having a repertoire of mental strategies to solve calculations e.g. 14 + 6 = 20 therefore 20 - 6 = 14

bridging 10 / bridging 20

adding 9 by +10 & -1

vi. Making use of informal jottings such as blank number lines to assist in calculations with larger numbers e.g. 83 - 18 = 65



- vii. Solving one-step word problems (either mentally of with jottings) by identifying which operation to use, drawing upon knowledge of number bonds and explaining their reasoning
- viii. Beginning to present calculations in a horizontal format and explain mental steps using numbers, symbols or words
- ix. Learn to estimate/approximate first e.g. 29 + 30 (round to the nearest 10, the answer will be near 60)

Place value will be taught by counting on and counting back depending on the numbers.

Numbers such as 10, 100 and 1000 will be called Landmark Numbers.

When are children ready for written calculation?

Addition and Subtraction

- Do they know addition and subtraction facts to 20?
- Do they know place value and can they partition numbers in a variety of ways?
 E.g. 12 = 10 + 2, 12 = 9 + 3 12 = 8 + 4
- Can they add three single digit numbers mentally?
- Can they add and subtract any pair of two digit numbers mentally?
- Can they explain their mental strategies orally and record them using informal jottings?

Multiplication and Division

- Do they know their 2,3,4,5 and 10 time tables?
- Do they know the result of multiplying by 0 and 1?
- Do they understand 0 as a placeholder?
- Can they multiply two and three digit numbers 10 and 100?
- Can they double and halve two digit numbers mentally?
- Can they use multiplication facts they know to derive mentally other multiplication facts that they do not now
- Can they explain their mental strategies orally and record them using informal jottings?

The above lists are not exhaustive but are a guide for the teacher to judge when a child is ready to move from informal to formal methods of calculation.

Stages in Addition - (Please refer to the Visual Calculation for a more detailed breakdown)

1. Mental method, using partitioning:

Or

$$47 + 76 = (47 + 70) + 6$$

2. Introduction to vertical layout, using partitioning:

3. Vertical layout, expanded working, adding the least significant digit first:

47 + <u>76</u> 13 <u>110</u> 123 368 + <u>493</u> 11 150 <u>700</u> 861

4. Vertical layout, contracting the working to compact efficient form:

+ <u>76</u> 13 <u>110</u> 123

861

368 - 493 - 11 - 861

5. Moving on to larger numbers and decimals, before moving onto more abstract forms such as algebra and fractions.

Stages in Subtraction - (Please refer to the Visual Calculation for a more detailed breakdown)

ue	ranea bi eakaowii)					
	1. Methods using decomposition					
	89 - 65		563 -241			
	80 9 - <u>60 5</u> <u>20 4</u> = 24	-	500 60 3 200 40 1 300 20 2 = 322			
	Leading to:					
	89		563			
	- <u>65</u> <u>24</u>	-	<u>241</u>			
	<u>24</u>		<u>322</u>			

2. Vertical layout using expanded partitioning:

3. Using vertical layout, contracting the working moving to a compact efficient form:

Stages in Multiplication

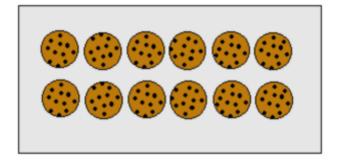
To multiply successfully, children need to be able to:

- recall all multiplication facts to 10 × 10
- partition number into multiples of one hundred, ten and one
- work out products such as 70×5 , 70×50 , 700×5 or 700×50 using the related fact 7×5 and their knowledge of place value
- add two or more single-digit numbers mentally
- add multiples of 10 (such as 60 + 70) or of 100 (such as 600 + 700) using the related addition fact, 6 + 7, and their knowledge of place value
- add combinations of whole numbers using the column method (see above).

Note: It is important that children's mental methods of calculation are practised and secured alongside their learning and use of an efficient written method for multiplication.

1. Arrays. Children can start in Key Stage 1 to understand the concept of multiplications by using arrays. Arrays can help your children develop concepts of multiplication and division.

The teacher will say, "An array shows objects in rows and columns. The teacher will show an example of a row and column using an array illustration in this case cookies on a cookie sheet. $(2 \times 6 = 12)$



2. Repeated Addition:

You know, a cat has four legs. Suppose there are 3 cats. How many legs are there altogether?

The answer is 4 + 4 + 4. Using our knowledge of addition, we can find this repeated addition as 4 + 4 + 4 = 12 or 3 + 4 + 4 = 12.

210 + 55

266

3. Mental Method using partitioning, multiplying tens first:

$$38 \times 7 = (30 \times 7) + (8 \times 7) = 210 + 56 = 266$$

4. Grid Layout Method (2 digit by 1 digit):

5. Grid Layout Method (3 digit by 1 digit) i.e. 238×7 :

X	200	30	8	1400 210
7	1400	210	56	+ 56
				1666

6. Grid Layout extended to bigger numbers (ThHTU)

i.e.
$$56 \times 27 = (50 + 6) \times (20 + 7)$$

X	50	6	
20	1000	120	1120 392
7	350	42	
<u>'</u>			1512

7. Vertical Format, expanded working:

8. Extended to HTU x U

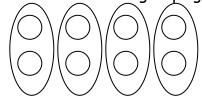
Long Multiplication

9. Vertical Format, compact working:

Stages in Division

To introduce division it should be practical, using equipment to demonstrate. Children in Key Stage 1 are to understand division as grouping and sharing which is repeated subtraction

1. Number lines and grouping:



2. Informal methods using multiples of the divisor or 'chunking' TU ÷ U:

Answer: 14 r 2

3. 'Chunking' HTU ÷ U

Answer: 36 r 4

4. Efficient 'Chunking' HTU ÷ U

Answer: 32 r 4

5. Extending to decimals with up to 1 place

<u>Answer: 12.5</u>

6. Chunking Extended HTU ÷ TU (Efficiently developed):

<u>Answer: 23 r 8</u>

7. Extending to an efficient standard method:

<u>Answer: 23 r 8</u>

8. Partitioning standard method:

Answer: 23 r 8

9. Extend to Compact Method

<u>Answer: 23 r 8</u>

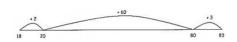
Addition

TU +TU developing to HTU +TU or HTU +

1. Use number lines to count on.

У3

HTU



2. Horizontal expanded method, using partitioning.

$$47 + 76 = (40 + 70) + (7 + 6)$$

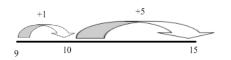
Or

3. Vertical expanded method adding least significant digit first.

Subtraction

TU - TU, developing to HTU -TU or HTU - HTU.

1. Use a number line to count up.



2. Decomposition using expanded form 89 - 65

3. Use vertical form (expanded partitioning)

y4 HTU + TU then HTU + HTU

1. Vertical expanded method adding least significant digit first.

HTU - TU then HTU - HTU

1. Decomposition using expanded form. 89 - 65

2. Decomposition using compact form.

	Addition	Subtraction
	2. Leading to 'carrying' above the line.	85 - 69
	368	
	+ 93	78 ₁5
	11	- <u>69</u>
	<u>461</u>	<u>16</u>
	3. Calculations extending to include	2 Calculations autonolina to include
	addition of two or more 3-digit sums of	3. Calculations extending to include
	money.	addition of two or more 3-digit sums of
	£3.68	money.
	+ 93	£2 3 .168
	11	- <u>1.93</u>
	£4.61	£ 1.75
У5	HTU + HTU then ThHTU + ThHTU	HTU - HTU the ThHTU - ThHTU
. •	1. Vertical expanded method adding	. Decomposition using expanded form.
	least significant digit first.	189 - 165
	1,356	
	+ <u>2,487</u>	100 80 9
	13	- <u>100 60 5</u>
	130	0 60 4 = 24
	700	<u> </u>
	3000	2. Decomposition using compact form.
	3843	185 - 169
	2. Leading to compact written method	1 78 15
	'carrying' above the line.	- <u>169</u>
	1,356	<u>16</u>
	2,487	_
	11	3. Calculations extending to include
	<u>3843</u>	subtraction of decimals, with up to 3
		digits & and the same number of decimal
	3. Calculations extended to include	places, in expanded format leading to
	addition of two of more decimal	vertical format.
	fractions, with up to 3 digits and same	
	number of decimal places, in vertical	
	format	
У6	Th HTU + ThHTU & then any number of	ThHTU - THHTU & then any number of
	digits.	digits
	1. Compact written method 'carrying'	1. Decomposition using compact form.
	I	I .
	above the line.	
	above the line. 1,356	1 2 ,12 3 145
		1 2 , ₁₂ 3 145 <u>1</u> ,765
	1,356	•

Addition	Subtraction
2. Calculations extended to include addition of two or more decimal fractions with up to for digits & either one or two decimal places.	2. Calculations extended to include subtraction of two or more decimal fractions with up to 3 digits & either one or two decimal places in vertical format.
and an analysis product	

	Multiplication	Division		
K51	Arrays and Repeated Addition	Arrays, Number Lines Grouping and Sharing		
У3	Mental Method using partitioning, multiplying tens first:	Informal methods using multiples of the divisor or 'chunking' TU ÷ U:		
	38 x 7 = (30 x 7) + (8 x 7) = 210 + 56 = 266 Grid Layout Method (2 digit by 1 digit):	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		
	X 30 8 210 7 210 56 + 56 266			
У4	Grid Layout Method (3 digit by 1 digit) i.e. 238 x 7:	'Chunking' HTU ÷ U i.e 256 ÷ 7		
	X 200 30 8 7 1400 210 56 1400 210 56	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		
	1666	$\frac{-42}{4} \frac{42}{36} \frac{36}{3}$		

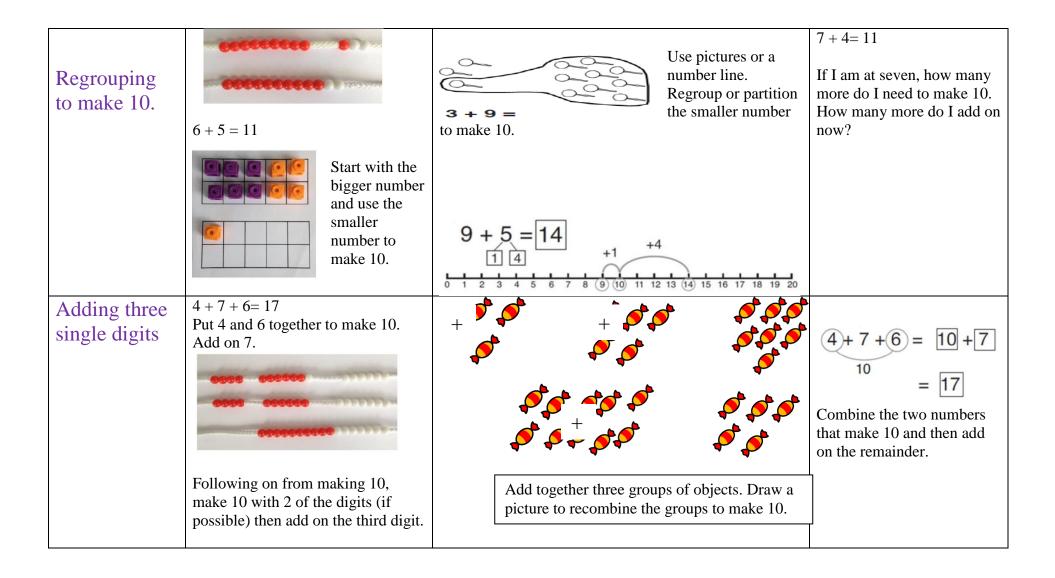
У5		extended to s (ThHTU)	bigger	Extending	to decimals	with up	to 1 pla	ace
	i.e. 56 × 27 = (50 + 6) × (20 + 7)			87.5 ÷ 7	87.5 <u>- 70.0</u>	70 =	10	x 7
	1.0. 30 %	(2) - (30 · (), x (20 · /)		17.5	70-		
	X	50	6		- <u>14.0</u> 3.5	14 =	2	× 7
					3.5_	3.5 =	0.5	x 7

	20	1000	120	0	1	12.5
	7	350	42	Chunking Extended F	TU ÷ TU (E	fficiently
У6		350 mat, expanded		560 ÷ 24 560 - 480 80	72 =	20 x 24 3 x 24 23
70	Ver ricui y or r	38 X 7 210 56 266		method: 560 ÷ 24 24)560 - 480 80 -72	20	
	Extended to Long Mul	HTU x U tiplication		8	23	
	56 X 27 1000 120 350 42 1512	(6 (50	0 × 20) × 20) 0 × 7) × 7)	Partitioning standard 560 ÷ 24 24)56 10 + 10 + 24 240 + 240 +	3 r 8 80	
	56 X 27 1120 392 1512 1		working: 6 × 20) 6 × 7)	2 3 560 ÷ 24 24) 5 5 6 86	<u>r</u> 8	

<u>Progression in Calculations</u>

Addition

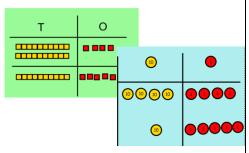
Objective and	Concrete	Pictorial	Abstract
Strategies			
Combining two parts to make a whole: part- whole model	Use cubes to add two numbers together as a group or in a bar.	Use pictures to add two numbers together as a group or in a bar.	4 + 3 = 7 $10 = 6 + 4$ 3 Use the part-part whole diagram as shown above to move into the abstract.
Starting at the bigger number and counting on	, 000000000000000000000000000000000000	12 + 5 = 17	5 + 12 = 17
counting on		10 11 12 13 14 15 16 17 18 19 20	
	Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	Start at the larger number on the number line and count on in ones or in one jump to find the answer.	Place the larger number in your head and count on the smaller number to find your answer.



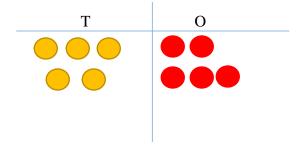
Column method- no regrouping

24 + 15=

Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.



After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions.

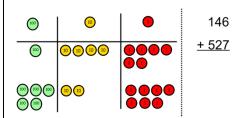


Calculations

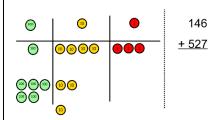
21

Column methodregrouping

Make both numbers on a place value grid.

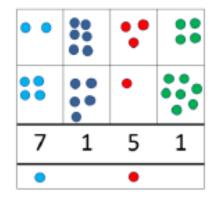


Add up the units and exchange 10 ones for one 10.



Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added.

Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding.



Start by partitioning the numbers before moving on to clearly show the exchange below the addition.

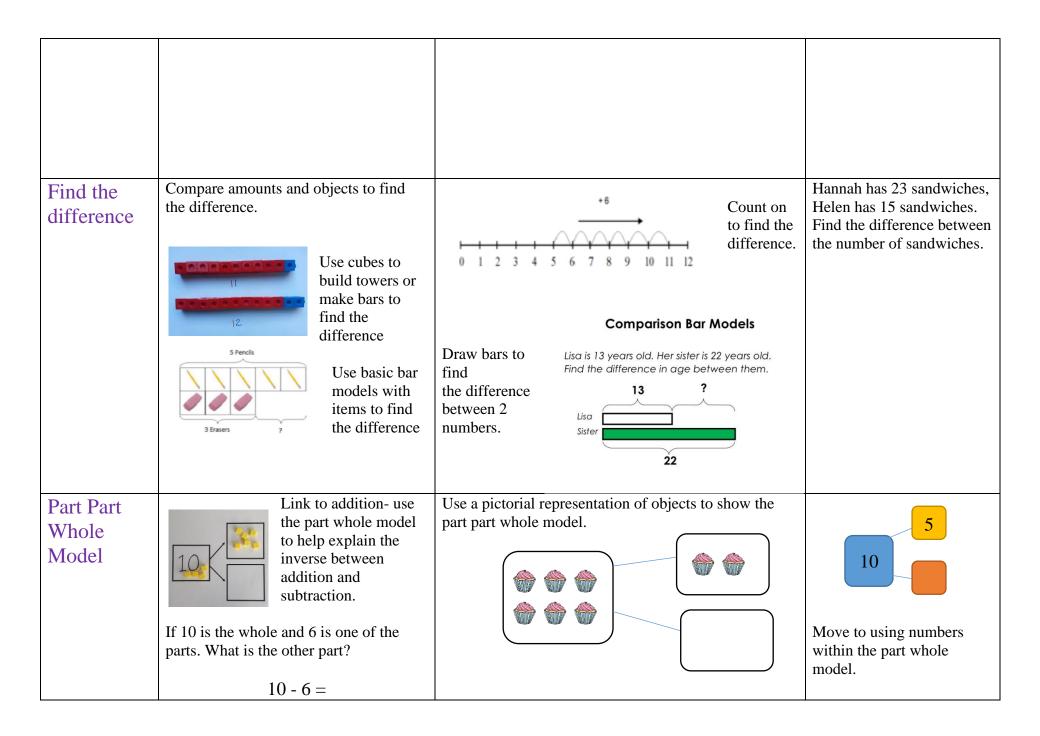
$$\begin{array}{rrrr} 20 & + & 5 \\ \underline{40} & + & \underline{8} \\ 60 & + & 13 & = 73 \end{array}$$

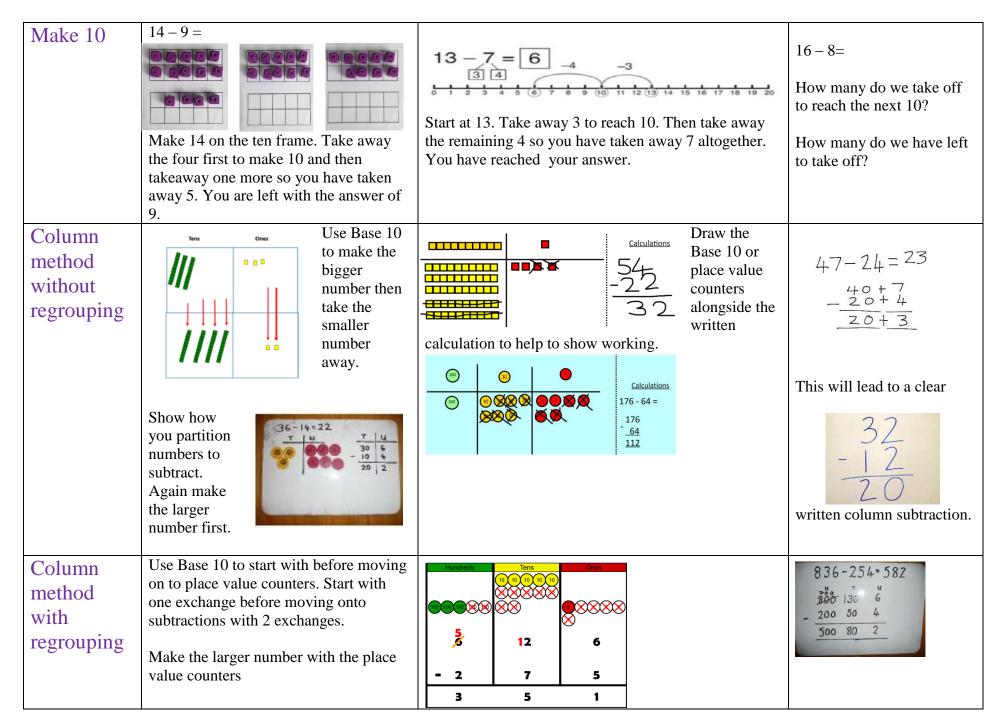
$$\frac{536}{+85}$$
 $\frac{621}{11}$

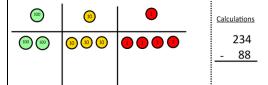
This can also be done with Base 10	As the children move on,
to help children clearly see that 10	introduce decimals with the
ones equal 1 ten and 10 tens equal	same number of decimal
100.	places and different. Money
	can be used here.
As children move on to decimals,	
money and decimal place value	
counters can be used to support	
learning.	72.8
	+ 54.6
	127.4 £ 2 3 . 5 9
	+ t 7 . 5 5
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
	2 3 . 3 6 1
	9 . 0 8 0
	5 9 . 7 7 0
	<u>+ 1 . 3 0 0</u>
	9 3 . 5 1 1

Subtraction

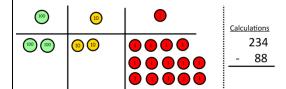
Subtraction			
Objective	Concrete	Pictorial	Abstract
and			
Strategies			
Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away.	Cross out drawn objects to show what has been taken away.	18 -3= 15
	6-2=4	$ \begin{array}{cccc} \stackrel{\wedge}{\wedge} & \stackrel{\wedge}{\wedge} & \stackrel{\wedge}{\wedge} & \stackrel{\wedge}{\wedge} \\ \stackrel{\wedge}{\wedge} & \stackrel{\wedge}{\wedge} & \stackrel{\wedge}{\wedge} & \stackrel{\wedge}{\wedge} & \stackrel{\wedge}{\wedge} \\ \stackrel{\wedge}{\wedge} & \stackrel{\wedge}{\wedge} & \stackrel{\wedge}{\wedge} & \stackrel{\wedge}{\wedge} & \stackrel{\wedge}{\wedge} \\ 15 - 3 = 12 \end{array} $	8 - 2 = 6
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones.	Count back on a number line or number track 9 10 11 12 13 14 15 Start at the bigger number and count back the smaller	Put 13 in your head, count back 4. What number are you at? Use your fingers to help.
	Use counters and move them away from the group as you take them away counting backwards as you go.	number showing the jumps on the number line. -10 -10 -10 -10 -10 -10 -10 -10 -10 -1	



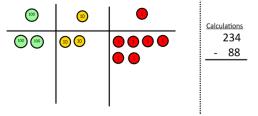




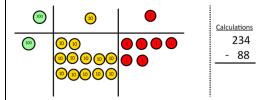
Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.



Now I can subtract my ones.



Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.



Now I can take away eight tens and complete my subtraction

Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.

When confident, children can find their own way to record the exchange/regrouping.



Just writing the numbers as shown here shows that the child understands the method and knows when to exchange/regroup. Children can start their formal written method by partitioning the number into clear place value columns.

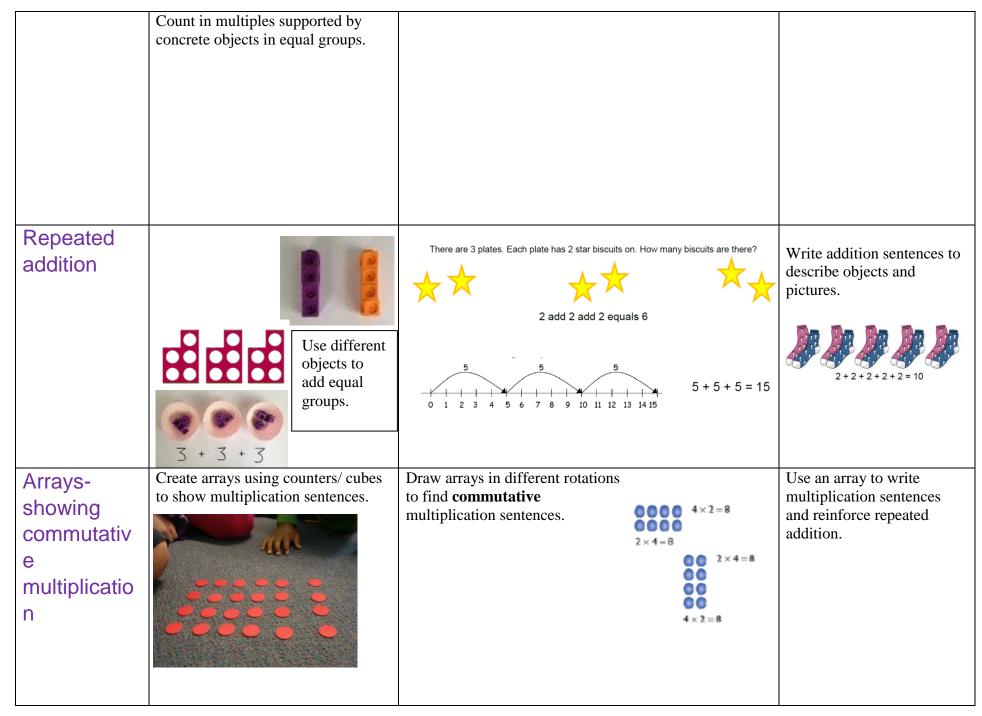


Moving forward the children use a more compact method.

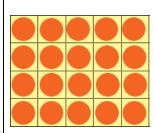
This will lead to an understanding of subtracting any number including decimals.

Multiplication

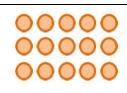
Mulupheation			1
Objective and	Concrete	Pictorial	Abstract
Strategies			
Doubling	Use practical activities to show how to double a number.	Draw pictures to show how to double a number.	16
		Double 4 is 8	10 6 1 _{x2} 1 _{x2}
	double 4 is 8 $4 \times 2 = 8$		20 12 Partition a number and then double each part before
			recombining it back together.
Counting in multiples	to the second	Sus our Sur our Sur our	Count in multiples of a number aloud. Write sequences with multiples of numbers.
		0 5 10 15 20 25 30	2, 4, 6, 8, 10
		Use a number line or pictures to continue support in counting in multiples.	5, 10, 15, 20, 25, 30



Gric	l Me	th



Link arrays to area of rectangles.



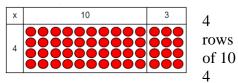
$$5 + 5 + 5 = 15$$

 $3 + 3 + 3 + 3 + 3 = 15$
 $5 \times 3 = 15$

 $3 \times 5 = 15$

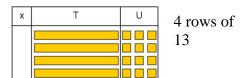
nod

Show the link with arrays to first introduce the grid method.



rows of 3

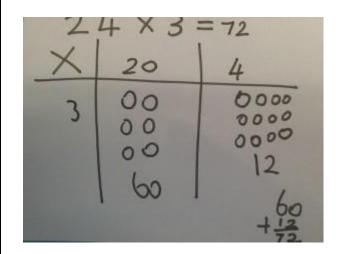
Move on to using Base 10 to move towards a more compact method.



Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.

Children can represent the work they have done with place value counters in a way that they understand.

They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.

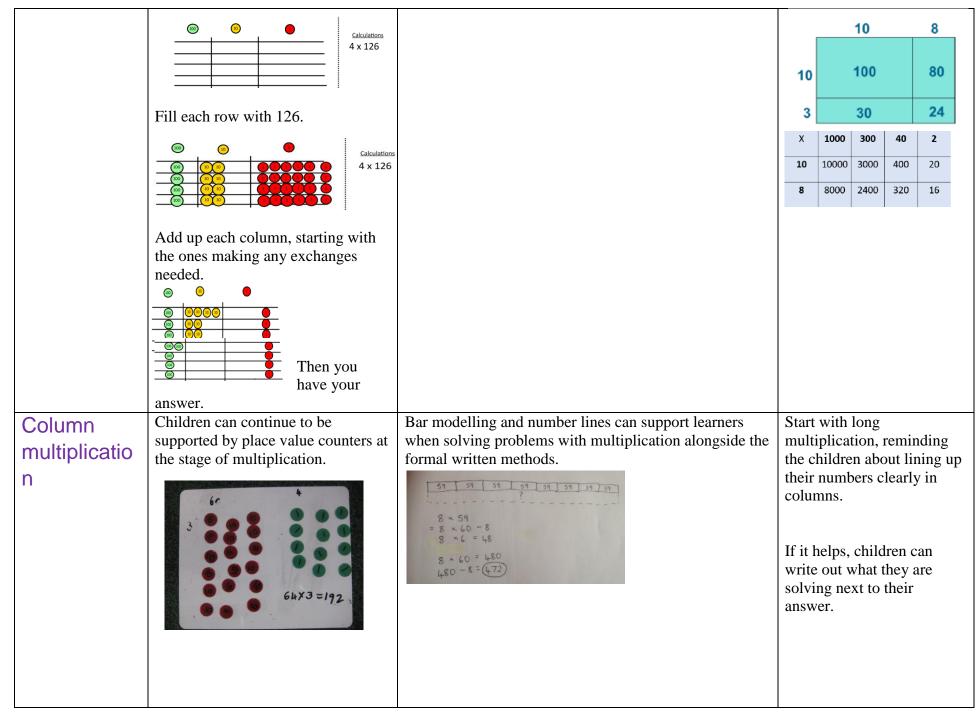


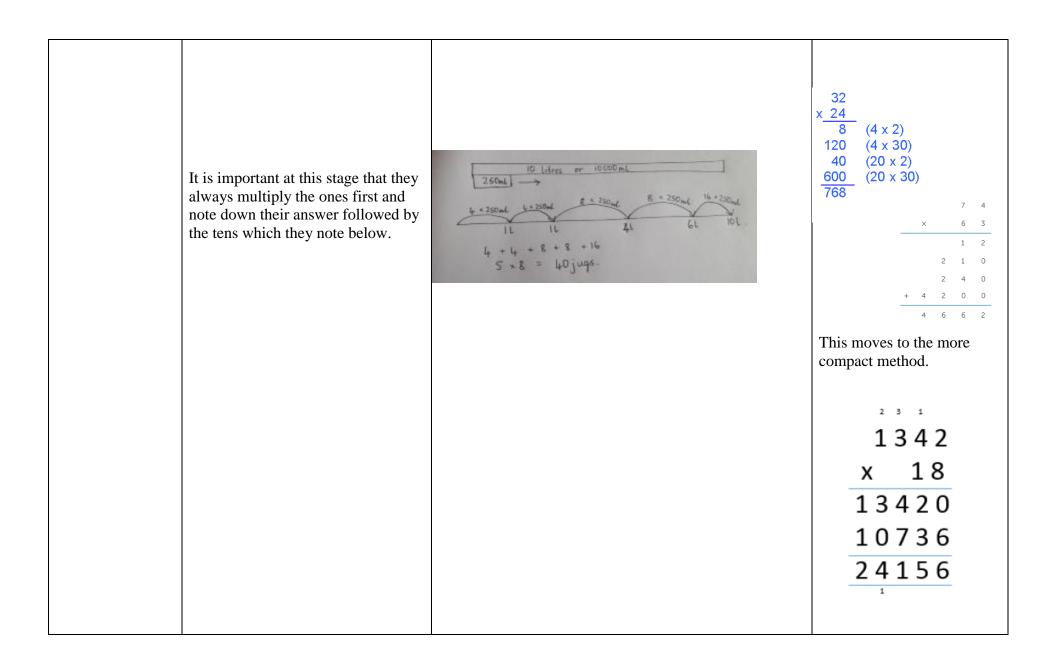
Start with multiplying by one digit numbers and showing the clear addition alongside the grid.

×	30	5
7	210	35

$$210 + 35 = 245$$

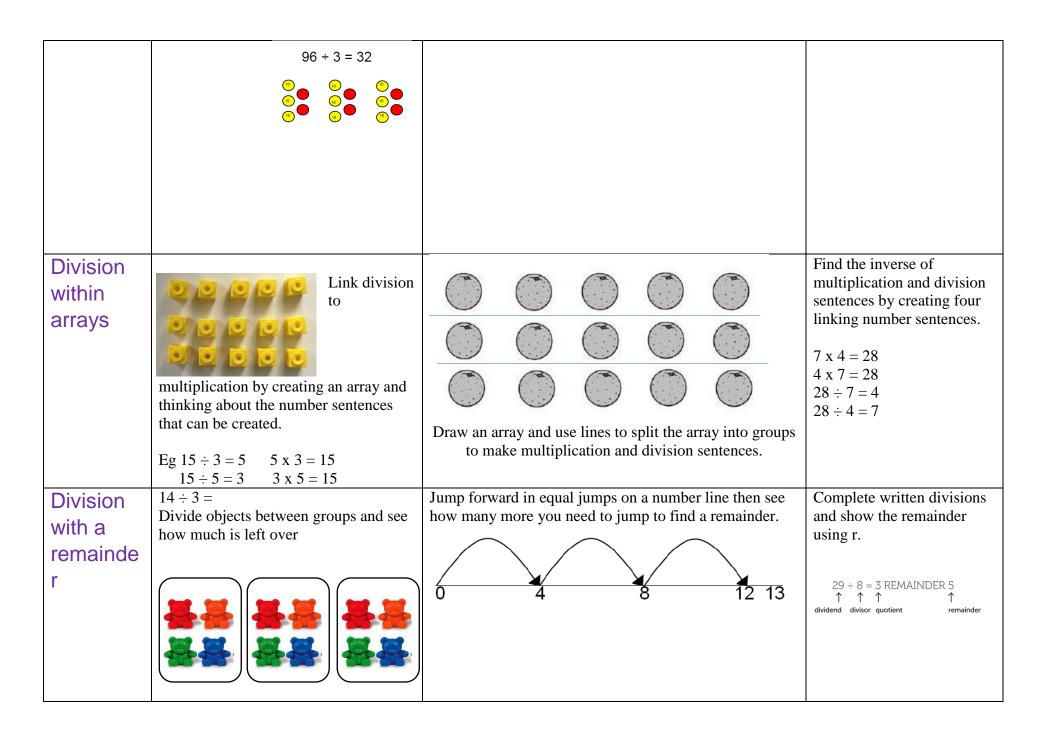
Moving forward, multiply by a 2 digit number showing the different rows within the grid method.

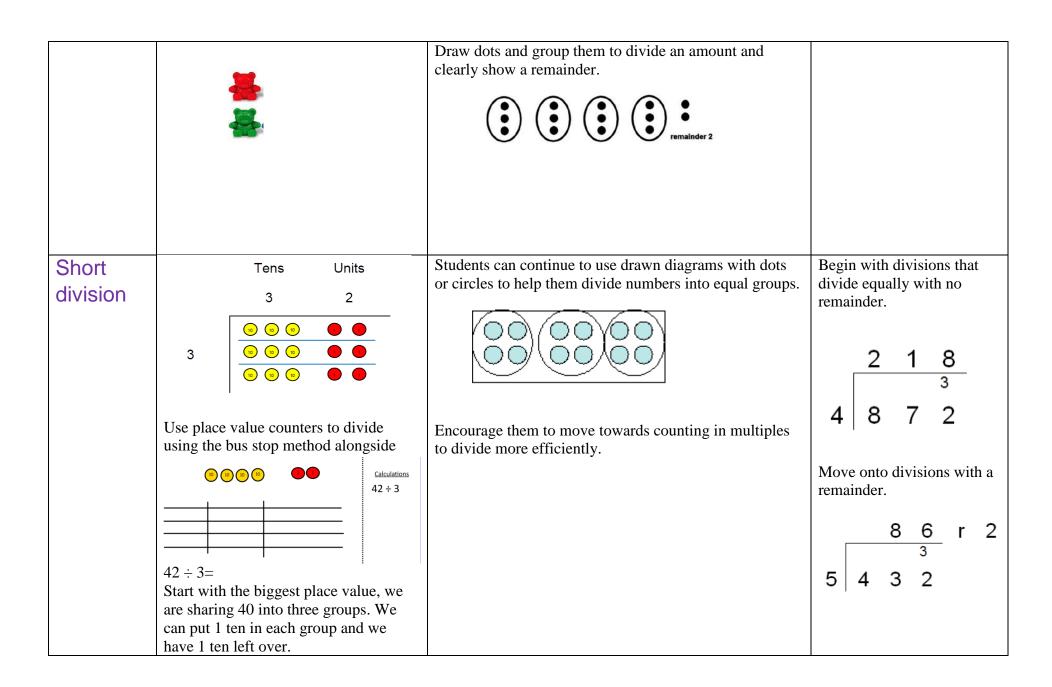


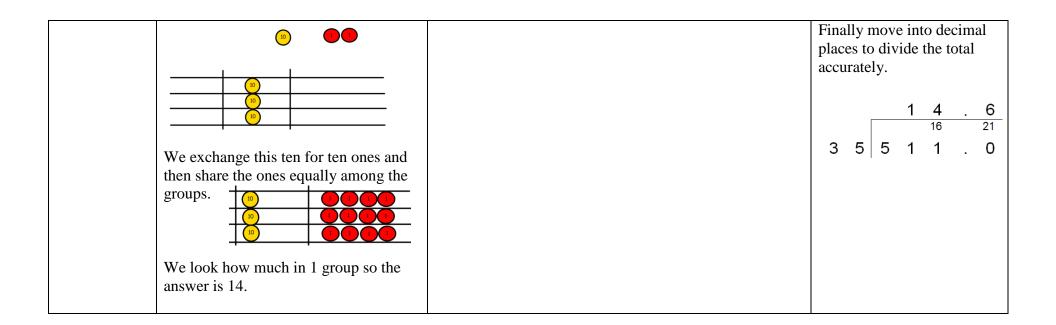


Division

DIVISION		D' 1	A1 /
Objective	Concrete	Pictorial	Abstract
and			
Strategies Sharing objects into groups	I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities. $8 \div 2 = 4$	Share 9 buns between three people. $9 \div 3 = 3$
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.	Use a number line to show jumps in groups. The number of jumps equals the number of groups. 0 1 2 3 4 5 6 7 8 9 10 11 12 3 3 3 3 Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?
		20 ? 20 ÷ 5 = ? 5 x ? = 20	







Arithmetic

Addition

Ensure that you use your place value to arrange your columns accurately.



When adding values you may need to carry. If the values in a column add up to 10 or more you will need to carry.

Example: In the units column 2 and 8 equal 10 so 0 goes in the units column and the 1 is carried.

If the values you are adding have a different amount of decimal places, ensure that the decimal point is in a column.

If you need to, add placeholders into empty columns.



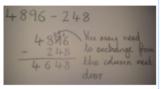


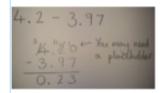
Some addition may be done mentally; however it is also fine to use columns. Watch out for crossing boundaries as they can lead to careless errors.

Subtraction

When subtracting, if the number on the bottom is larger than the one on the top, you may need exchange from the column next door.

If the column has a 9 you will change it to an 8 and carry 1 down.

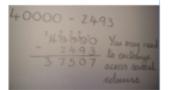




If the number you are subtracting has more decimal places than the one you are subtracting from you will need to add placeholders and exchange.

If you are subtracting from a number with lots of zeroes you will need to exchange across several columns.

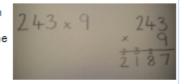
Example: The 4 in 40000 has been changed to a 3 and the column next door is changed to 10. This is then changed to a 9 and 1 is exchanged to the column next door.

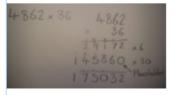


Multiplication

One of the most obvious questions on your SATs will be a straight tables problem e.g. 7 x 8 or 11 x 12

When multiplying values we can use columns. In this case we would multiply each part of 243 by 9. If the answer is greater than 10 we carry to the column next door.

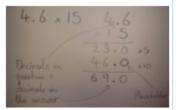


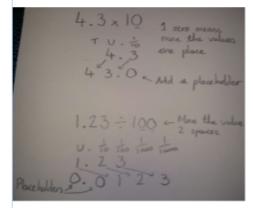


If you are multiplying by a two-digit number, you multiply by the units and then the tens column. When multiplying by the tens column we add a zero first. Finally, we add them together.

When multiplying a whole number by a decimal you need to place decimal points in the answers in the same place as the question.

Don't forget that we still need a place holder when multiplying by tens.





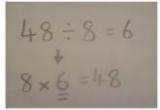
If you are multiplying or dividing by 10, 100 or 1000 you will be moving the digits.

Write the number you are dividing (the dividend) under the correct place value.

Count the number of zeroes in the number you are dividing by (the divisor). Then move the dividend this many places.

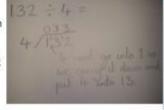
If it is multiplying the value gets bigger; if it is division it gets smaller.

You may need to add place holders in any empty spaces.



For some division problems we can use our multiplication knowledge to solve the problem. For example, we know that 48 ÷ 8 = 6 because we know that $8 \times 6 = 48$

If we are dividing a larger number by a single digit we can use the short division (bus stop) method. We write our dividend (the number being divided up) in the bus stop and our divisor outside. We then try to put the divisor into each value in turn. If the divisor goes into the value we write the amount of times above and then carry any left over to the next column.



In the example 4 didn't go into 1 so we put a zero and carried the 1 down, 4 into 13 three times with one left over. Therefore we wrote 3 above and

carried one down again.

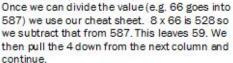
Sometimes we are left with some of our original value which can't be divided up any further using whole numbers. For example if I was dividing 7 by 4. I would have 3 left over. This can be written as a remainder or we can convert into a decimal.

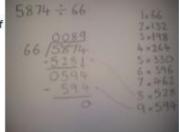
We do this by adding a decimal point and a zero to our dividend and then carrying the remainder into this column.

In this example the remainder was 4: however we carried it down to become 40 which is a multiple of our divisor, 8, so we can divide.

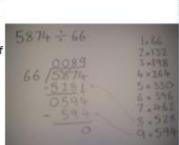
Long division is needed when we are dividing by 2-digit numbers or more. To help out we write a 'cheat sheet' for the divisor e.g. the 66 times tables in our example.

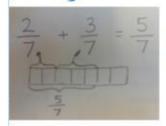
We then use this to help divide up the number. If it will not divide (e.g. 66 cannot go into 5) we write zero above then use the 8 with the 5 to make 58. If the divisor still will not go in we continue this process until it will.





This process can be tricky and it takes time so you need to concentrate.

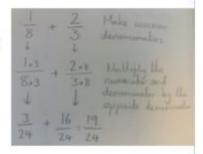


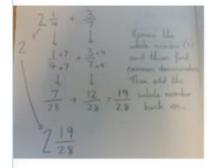


If you are adding fractions with common denominators, you simply add the numerators. For example 3/4 of a pie added to 1/4 of a pie is 4/4 o the pie.

If your denominators are not the same, you can force them to be common by multiplying them by one another. Just remember that whatever you do to the denominator, you also do to the numerator.

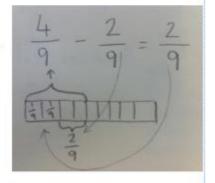
Once the denominators are the same, they can be easily added using the method above.



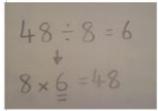


Sometimes you will be working with mixed number (e.g. one and a half) and a fraction. If you are adding and they do not have common denominators, simply remove the whole number (2) for now. Use the methods above to force common denominators and add the fractions. Finally bring the 2 wholes back and add them on.

Subtracting fractions with common denominators is just like adding; we simply work with the numerators.

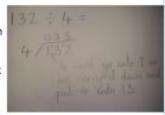


Division



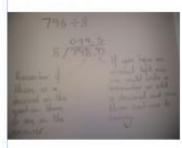
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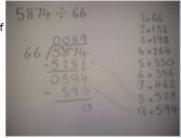
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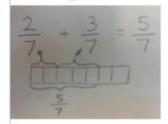
We then use this to help divide up the number. If it will not divide (e.g. 66 cannot go into 5) we write zero above then use the 8 with the 5 to make 58. If the divisor still will not go in we continue this process until it will.

Once we can divide the value (e.g. 66 goes into 587) we use our cheat sheet. 8 x 66 is 528 so we subtract that from 587. This leaves 59. We then pull the 4 down from the next column and continue.

This process can be tricky and it takes time so you need to concentrate.



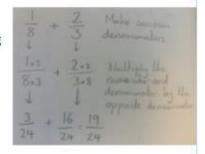
Working with fractions

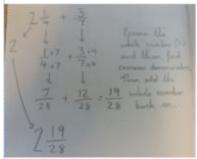


If you are adding fractions with common denominators, you simply add the numerators. For example 3/4 of a pie added to 1/4 of a pie is 4/4 o the pie.

If your denominators are not the same, you can force them to be common by multiplying them by one another. Just remember that whatever you do to the denominator, you also do to the numerator.

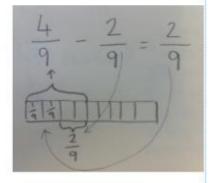
Once the denominators are the same, they can be easily added using the method above.



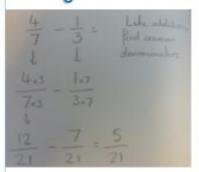


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Subtracting fractions with common denominators is just like adding: we simply work with the numerators.



Working with fractions

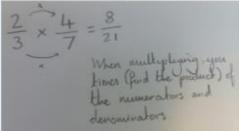


Subtracting fractions is also like adding given that we force common denominators, then we work with the numerators.

If you are working with mixed numbers (whole numbers and fractions e.g. one and a half) you may need to convert the mixed number into an improper fraction (where the numerator is greater than the denominator). We do this by multiplying the whole number by the denominator and then adding the numerator.

denominators and calculate.

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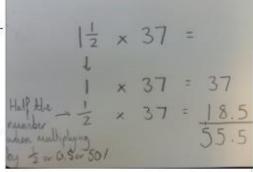
Multiplying to fractions by one another is nice and straight forward. We simply multiply the numerators by one another and do the same with the denominators.

When you multiply by a whole number, simply multiply the numerator by the whole number.

Working with fractions

Multiplying a mixed number can be trickier. However, simply partition the mixed number into its whole number and fraction and multiply each individual.

Remember that if you multiply a number by a half it halves the number e.g. $10 \times 1/2 = 5$ Once you have multiplied both parts, add the answers together.



If the numerator will divide by the whole number, we do that.

If it would be 3 would divide by 4 to leave a whole number) we rulliply by the donominator

When dividing fraction by a whole number it all depends on whether the numerator is a multiple of the divisor. If it is, you just divide it e.g. in the example 4 is a multiple of 2 so it will divide.

If it will not (as in example 2) then we multiply the denominator instead.

Dividing two fractions can be confusing but relates to our other methods. We inert (flip) the second fraction. Then we multiply the numerators and denominators.

4 :
$$\frac{6}{9}$$
 = lf we are dividing two fractions, we work the 2nd fraction (Fup it)

4 : $\frac{9}{6}$ = $\frac{36}{48}$ the numerators and denominators.

Finding percentages of numbers

Percentage relates to parts of 100. Sometimes we ned to calculate a parentage using our division methods.

30% of 360

If we need to find a percentage which is a multiple of 10 (e.g. 30%) we will need to find 10%.

We find 10% by dividing the number by 10. This involves moving the digits one place to the right.

360 ÷ 10 = 36

36 = 10%

If we multiply the answer by 3 we will get 30%

36 x 3 = 30%

 $36 \times 3 = 108$

30% of 380 = 108

32% of 360

If the value is not multiple of 10 (e.g. 32%) we can find 1% and then multiply by the amount we need (32%)

 $360 \div 100 = 3.6$

 $3.6 \times 32 = 115.2$

Alternatively, we could partition the percentage. We can work out parts and add them together

10% = 36 10% = 36 10% = 36 1% = 3.6 1% = 3.6

32%

= 115.2

Finding fractions of numbers

We can find fractions of whole numbers by using the numerator and denominator.

3/5 of 60

First we divide the amount by the denominator.

 $60 \div 5 = 12$

Then we multiply by the numerator

 $12 \times 3 = 36$

Therefore 3/5 of 60 = 36

Finding the mean

The mean is another word for the average. We find the mean of a set of data by adding the values together and dividing by how many values there were.

5

For example, here is a set of data containing 5 values.

4 6

Added together they total 20. We divide this total by 5.

 $20 \div 5 = 4$

So the mean average of the data is 4.

BIDMAS/BODMAS

Some calculations need to be done in specific order.

B = Brackets

I/O = Indices or orders e.g. 4 squared

D = Division M = Multiplication (Done from left to right)

A = Addition S = Subtraction (Done from left to right)

Example

2 + 3 x 4 (We do the multiplication before addition)

2 + 12 = 14

32 + (4-1) (First we solve the brackets, then the indices)

 $3^2 + 3$

9 + 3 = 12

Summary

- Progression is made when pupils are ready, though age related expectation will be followed throughout the school in line
 with the National Curriculum.
- The children will cover mathematics in three stages of understanding: fluency, reasoning and problem solving.
- Children should be persuaded to estimate first.
- Always check the answer, preferably using a different method e.g. inverse operation.
- Pay attention to language refer to actual value of digits.
- Children who make persistent mistakes should return to the method that they can use accurately until ready to move on.
 They will also be supported by the use of manipulatives and concrete objects.
- Children need to know number and multiplication facts by heart.
- Discuss errors and diagnose problems and then work through problem do not simply re-teach method.
- When revising or extending to more challenging or larger numbers, refer back to expanded methods. This helps reinforce
 understanding and reminds children that they have an alternative to fall back on if they are having difficulties.